

# Algorithmic Mechanisms for Internet Supercomputing under Unreliable Communication

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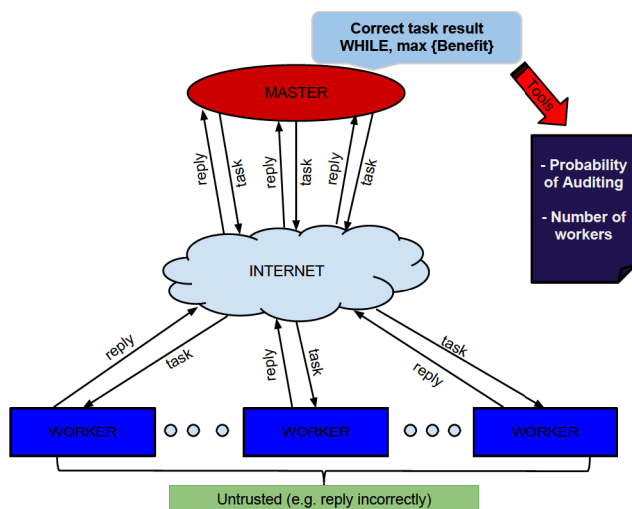
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## Motivation

- Internet emerges as a viable platform for supercomputing
  - @home systems, volunteering computing  
(e.g., SETI@home [Korpela et al 01])
  - P2P and Grid computing [Foster, Iamnitchi 03]
- Problem:** Great potentials of Internet-based computing limited by untrustworthy platforms components

## Motivation



## Background

### Definition

"A **game** consists of a set of players, a set of moves (or strategies) available to those players, and a specification of payoffs for each combination of strategies." [Wikipedia]

- Game Theory:
  - Players (processors) act on their self-interest
  - Rational behavior:  
seek to increase own utility choosing strategy according to payoffs
  - Protocol is given as a game
  - Design objective is to achieve **equilibrium** among players

## Background

### Definition

**Nash Equilibrium (NE)**: players do not increase their expected utility by changing strategy, if other players do not change [Nash 50]

- Algorithmic Mechanism Design [Nisan, Ronen 01]  
Games designed to provide **incentives** s.t. players act “correctly”
  - Behave well: **reward**
  - Otherwise: **penalize**
- The design objective is to induce a **desired** behavior (e.g. unique NE)

## Prior Work

In **Fernandez, Georgiou and Mosteiro 10** an Internet-based master-worker framework was considered

- Game-theoretic approach
- Types of workers:
  - **malicious**: always report incorrect result
  - **altruistic**: always compute and report correct result
  - **rational**: selfishly (in a game-theoretic sense) choose to be **honest** or **cheat**
- A reliable network was considered

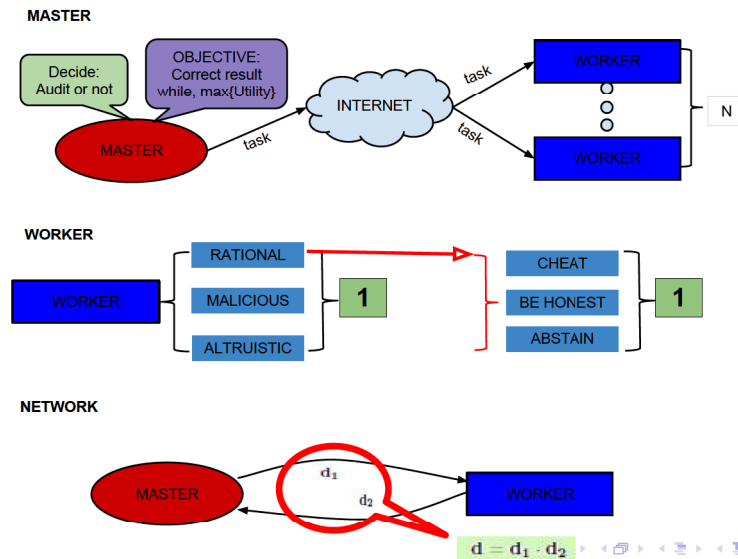
## Problem Statement

- Communication uncertainty
  - Messages exchanged may **get lost** or **arrive late**
- Possibility of workers not replying
  - Around 5% of the workers are available more than 80% of the time  
Half of the workers are available less than 40% of the time [Heien, Anderson and Hagihara 09]
  - Long computational length is incur by a task [Kondo et al. 07]
- **Master's challenges**
  - Provide incentives for **workers to reply and reply truthfully**
  - Ensure the above in the presence of **low network reliability**

## Contributions

- Develop and analyze two realistic game-theoretic mechanisms
  - **Time-based** mechanism
  - **Reply-based** mechanism
- Mechanisms provide the necessary incentives for rational workers to **truthfully compute and return the task result**, despite:
  - Malicious workers actions
  - Network unreliability
- Apply the mechanisms to two realistic settings:
  - **SETI-like** volunteer computing applications
  - **Contractor-based** applications (e.g. Amazons mechanical turk)

## Framework



## Framework General Protocol

- Master assigns a task to  $n$  workers
- Rational worker cheats with probability  $p_C$  (seeking a NE)
- Master audits the responses with probability  $p_A$
- If master audits (computes the task itself)
  - rewards honest workers and
  - penalizes the cheaters
- If master does not audit
  - Accepts value returned by majority of workers
  - Rewards/penalizes according to one of three models

$\mathcal{R}_m$	the master rewards the <b>majority</b> only
$\mathcal{R}_a$	the master rewards <b>all workers</b> whose reply was received
$\mathcal{R}_\emptyset$	the master rewards <b>no worker</b>

Note: reward models may be fixed exogenously or chosen by the master

## Algorithms

- Time-based protocol
  - Master **fixes a time  $T$** , once it is reached gathers all received replies
  - Ties are broken at random
- Reply-based protocol
  - Master **fixes  $k$** , minimum estimated number of replies, by **choosing  $n$**
  - **If** at least  $k$  replies are received, audit with  $p_A$
  - **Else** it does nothing, and incurs penalty  $MC_S$
- **Note:** Master based on statistics may have knowledge to only one of two settings

## Equilibria Conditions

**Guaranteeing :**  $P_{succ} \geq 1 - \varepsilon$  **While** maximizing  $U_M$

Pr(master obtains correct answer):

$$P_{succ} = \sum_{i=k}^n r_i (p_A + (1 - p_A)h_i)$$

E(utility of master):

$$\text{master's utility } U_M = - \sum_{i=0}^{k-1} r_i MC_S + \sum_{i=k}^n r_i (p_A \alpha_i + (1 - p_A) \beta_i)$$

Expected **utility of the worker** when choosing to be honest over cheating and be honest over not replying

$$\begin{aligned} \Delta U_{HC} &= \pi_H \cdot w_H - \pi_C \cdot w_C \geq 0 \\ \Delta U_{HN} &= \pi_H \cdot w_H - \pi_N \cdot w_N \geq 0 \end{aligned}$$

## Mechanism Design

Master protocol to chose  $p_A$

- **Free rationals** (master does not rely on rational workers )
  - Case 1: probability of malicious workers  $p_\mu$  **very large**, high  $p_A$

$$p_A \leftarrow 1 - \varepsilon / \sum_{i=k}^n r_i c_i$$

- Case 2: probability of altruistic workers  $p_\alpha$  **big**

$$p_A \leftarrow 0$$

- Case 3: rationals probability of being honest  $p_H$  **is 1**, even if  $p_A = 0$

$$p_A \leftarrow 0$$

- **Guided rationals** (force the behavior of rational workers)
  - Rationals enforced to reply correctly ( $p_C = 0$  and  $p_N = 0$ )
  - $p_A$  is set according to worker's **equilibria conditions** depending on the **reward model**

Navigation icons

## SETI-like Scenario

Volunteering Computing

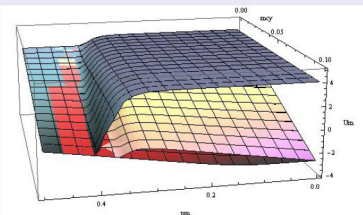
- each worker
  - incurs in no cost to perform the task ( $WC_T = 0$ )
  - obtains a benefit ( $WB_Y > WC_I = 0$ ) (recognition, prestige)
- master
  - incurs in a (possibly small) cost to reward a worker ( $MC_Y > 0$ ) (advertise participation)
  - may audit results at a cost ( $MC_A > 0$ )
  - obtains a benefit for correct result ( $MB_R > MC_Y$ )
  - suffers a cost for wrong result ( $MP_W > MC_A$ )
- $d > 0$ , as it is considered in the analysis as well
- Master can **choose**  $p_A$  and  $n$  so that  $U_M$  is maximized for  $P_{succ} \geq 1 - \varepsilon$  for any given worker-type distribution, reward model, and set of payoff parameters in the SETI scenario.

Navigation icons

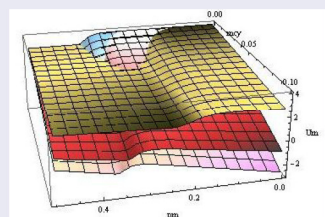
## SETI-like Scenario

Volunteering Computing

### Time-based Mechanism



- $d = 0.9$ ,  $n = 75$
- Upper plane  $\mathcal{R}_\emptyset$ , middle  $\mathcal{R}_m$  and lower plane  $\mathcal{R}_a$
- Master audits around  $p_\mu = 0.35$



- Reward model  $\mathcal{R}_m$ ,  $d = 0.9$
- Upper plane  $n = 15$ , middle  $n = 55$ , lower plane  $n = 75$
- For  $n = 15$ , earlier change to auditing strategy

Navigation icons

## SETI-like Scenario

Volunteering Computing

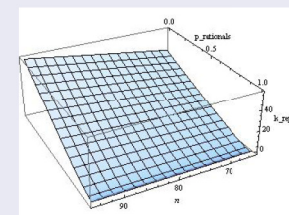
### Reply-based Mechanism

- $k \geq 1$
- Chernoff bounds for calculating  $k$

$$k = E - \sqrt{2E \ln(1/\zeta)}$$

with probability at least  $1 - \zeta$ ,  $0 < \zeta < 1$ , where  $E = nd(p_\alpha + p_\mu)$

- $\zeta = 1/n$  (used in plot)



- $n \in [65, 95]$ ,  $p_\rho \in [0, 1]$
- Appropriate value of  $n$  to get at least  $k$  replies
- $p_\rho$  increase,  $k$  decrease

Navigation icons

- A set of small navigation icons typically found in Beamer presentations, including symbols for back, forward, search, and other slide controls.

Thank you

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